

Point to Plane Distance

A Plane may be defined as:

$$Ax + By + Cz + D = 0$$

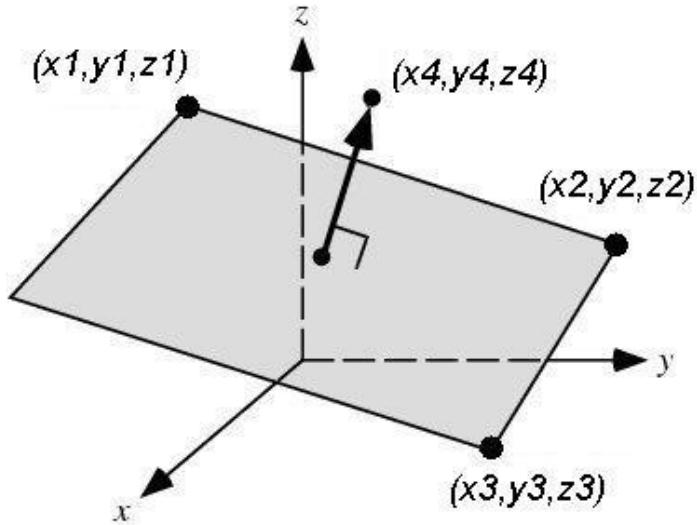
Where, given 3 points on that Plane (x_1, y_1, z_1) , (x_2, y_2, z_2) & (x_3, y_3, z_3) :

$$\begin{aligned} A &= y_1(z_2 - z_3) + y_2(z_3 - z_1) + y_3(z_1 - z_2) \\ B &= z_1(x_2 - x_3) + z_2(x_3 - x_1) + z_3(x_1 - x_2) \\ C &= x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2) \\ -D &= x_1(y_2z_3 - y_3z_2) + x_2(y_3z_1 - y_1z_3) + x_3(y_1z_2 - y_2z_1) \end{aligned}$$

Then,

$$D = -1(-D)$$

Diagram:



The perpendicular distance to a Point (x_4, y_4, z_4) to this Plane may be given as:

$$\frac{A(x_4) + B(y_4) + C(z_4) + D}{\sqrt{A^2 + B^2 + C^2}}$$